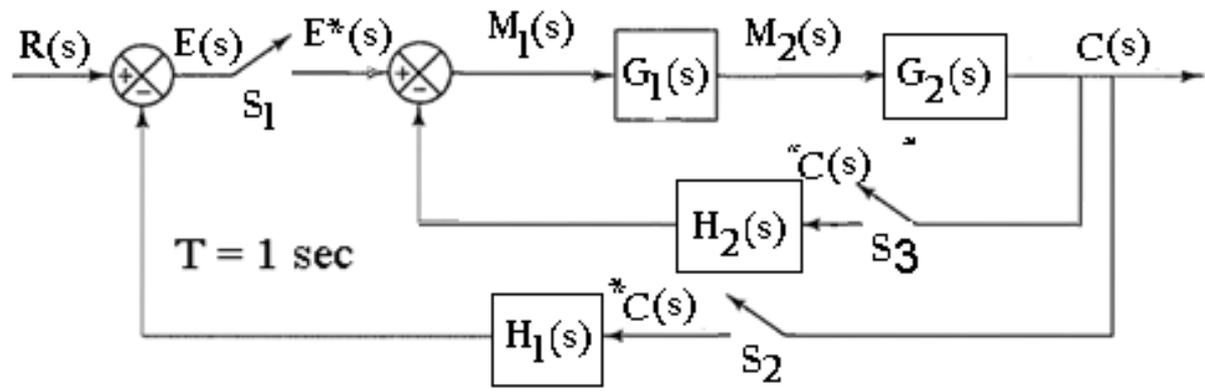


For the discrete data system shown below find:



Where $G_1(s) = \frac{1}{s+1}$, $G_2(s) = \frac{1}{s}$, $H_1(s) = 4$ (static gain) , $H_2(s) = \frac{s}{s+1}$

1. The pulse transfer function TF. (10 marks)
2. Describe the system output $C(z)$ when it is subjected to a unit step input.(10 marks)
3. Define the output sequence $c(k)$ of $C(z)$ (10 marks)
4. Find the initial and final values [$c(0)$ and $c(\infty)$]of the system. (10 marks)

Table of Laplace and Z-transforms

	$X(s)$	$x(t)$	$x(kT)$ or $x(k)$	$X(z)$
1.	-	-	Kronecker delta $\delta_0(k)$ 1 $k = 0$ 0 $k \neq 0$	1
2.	-	-	$\delta_0(n-k)$ 1 $n = k$ 0 $n \neq k$	z^{-k}
3.	$\frac{1}{s}$	$1(t)$	$1(k)$	$\frac{1}{1-z^{-1}}$
4.	$\frac{1}{s+a}$	e^{-at}	e^{-akT}	$\frac{1}{1-e^{-aT}z^{-1}}$
5.	$\frac{1}{s^2}$	t	kT	$\frac{Tz^{-1}}{(1-z^{-1})^2}$
6.	$\frac{1}{(s+a)^2}$	te^{-at}	kTe^{-akT}	$\frac{Tze^{-aT}z^{-1}}{(1-e^{-aT}z^{-1})^2}$
7.	$\frac{s}{(s+a)^2}$	$(1-at)e^{-at}$	$(1-akT)e^{-akT}$	$\frac{1-(1+aT)e^{-aT}z^{-1}}{(1-e^{-aT}z^{-1})^2}$
8.	-	-	a^k	$\frac{1}{1-az^{-1}}$
9.	-	-	a^{k-1} $k = 1, 2, 3, \dots$	$\frac{z^{-1}}{1-az^{-1}}$

The z transform is given as: $X(z) = \sum_{k=0}^{\infty} x(kT)z^{-k}$

Initial value: $x(0) = \lim_{z \rightarrow \infty} X(z)$

Final value theorem: $x(\infty) = \lim_{z \rightarrow 1} [(1-z^{-1})X(z)]$

ملاحظة: عوض عن e بقيمتها عند التحويل حيث:

$$e = 2.718 \text{ and } e^{-1} = 0.368$$