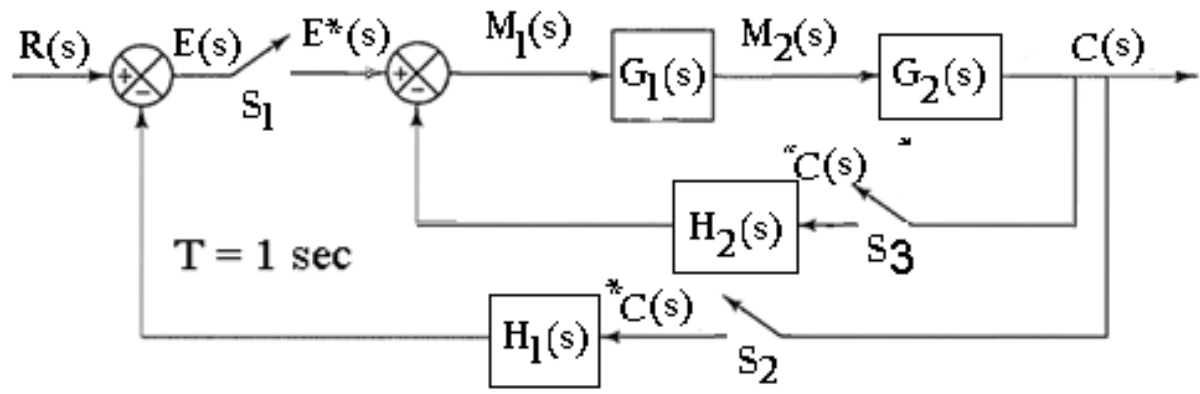


**For the discrete data system shown below find:**



Where  $G_1(s) = \frac{1}{s+1}$  ,  $G_2(s) = \frac{1}{s}$  ,  $H_1(s) = 4$  (static gain) ,  $H_2(s) = \frac{s}{s+1}$

1. The pulse transfer function TF. (10 marks)
2. Describe the system output  $C(z)$  when it is subjected to a unit step input.(10 marks)
3. Define the output sequence  $c(k)$  of  $C(z)$  (10 marks)
4. Find the initial and final values [ $c(0)$  and  $c(\infty)$ ] of the system. (10 marks)

**Table of Laplace and Z-transforms**

	$X(s)$	$x(t)$	$x(kT)$ or $x(k)$	$X(z)$
1.	-	-	Kronecker delta $\delta_0(k)$ 1 $k = 0$ 0 $k \neq 0$	1
2.	-	-	$\delta_0(n-k)$ 1 $n = k$ 0 $n \neq k$	$z^{-k}$
3.	$\frac{1}{s}$	$1(t)$	$1(k)$	$\frac{1}{1-z^{-1}}$
4.	$\frac{1}{s+a}$	$e^{-at}$	$e^{-akT}$	$\frac{1}{1-e^{-aT}z^{-1}}$
5.	$\frac{1}{s^2}$	$t$	$kT$	$\frac{Tz^{-1}}{(1-z^{-1})^2}$
6.	$\frac{1}{(s+a)^2}$	$te^{-at}$	$kTe^{-akT}$	$\frac{Te^{-aT}z^{-1}}{(1-e^{-aT}z^{-1})^2}$
7.	$\frac{s}{(s+a)^2}$	$(1-at)e^{-at}$	$(1-akT)e^{-akT}$	$\frac{1-(1+aT)e^{-aT}z^{-1}}{(1-e^{-aT}z^{-1})^2}$
8.	-	-	$a^k$	$\frac{1}{1-az^{-1}}$
9.	-	-	$a^{k-1}$ $k = 1, 2, 3, \dots$	$\frac{z^{-1}}{1-az^{-1}}$

The z transform is given as:  $X(z) = \sum_{k=0}^{\infty} x(kT)z^{-k}$

Initial value:  $x(0) = \lim_{z \rightarrow \infty} X(z)$

Final value theorem:  $x(\infty) = \lim_{z \rightarrow 1} [(1-z^{-1})X(z)]$

ملاحظة: عوض عن e بقيمتها عند التحويل حيث:

$e = 2.718$  and  $e^{-1} = 0.368$